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FISCAL POLICY SWITCHING IN JAPAN, THE U.S., AND THE U.K.

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Abstract

This paper estimates fiscal policy feedback rules in Japan, the United States, and the United Kingdom for more than a century, allowing for stochastic regime changes. Estimating a Markovswitching model by the Bayesian method, we find the following: First, the Japanese data clearly reject the view that the fiscal policy regime is fixed, i.e., that the Japanese government adopted a Richardian or a non-Richardian regime throughout the entire period. Instead, out results indicate a stochastic switch of the debt-GDP ratio between stationary and non-stationary even in the long run (i.e., globally non-stationary). Third, the Japanese result is in sharp contrast with the results for the U.S. and the U.K. which indicate that in these countries the government's fiscal behavior is consistently characterized by Richardian policy.

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Arata Ito Hitotsubashi University Graduate School of Economics 2-1 Naka, Kunitachi, Tokyo 186-8601, Japan b091110h@r.hit-u.ac.jp Fiscal Policy Switching in Japan, the U.S., and the U.K.*

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Abstract

This paper estimates fiscal policy feedback rules in Japan, the United States, and the United Kingdom for more than a century, allowing for stochastic regime changes. Estimating a Markovswitching model by the Bayesian method, we find the following: First, the Japanese data clearly reject the view that the fiscal policy regime is fixed, i.e., that the Japanese government adopted a Ricardian or a non-Ricardian regime throughout the entire period. Instead, our results indicate a stochastic switch of the debt-GDP ratio between stationary and nonstationary processes, and thus a stochastic switch between Ricardian and non-Ricardian regimes. Second, our simulation exercises using the estimated parameters and transition probabilities do not necessarily reject the possibility that the debt-GDP ratio may be nonstationary even in the long run (i.e., globally nonstationary). Third, the Japanese result is in sharp contrast with the results for the U.S. and the U.K. which indicate that in these countries the government's fiscal behavior is consistently characterized by Ricardian policy.

JEL Classification Numbers: E62

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Introduction 1

Recent studies about the conduct of monetary policy suggest that the scal policy regime has important implications for the choice of desirable monetary policy rules, particularly, monetary policy rules in the form of inflation targeting (Sims (2005), Benigno and Woodford (2007)). It seems safe to assume that scal policy is characterized as "Ricardian" in the terminology of Woodford (1995), or "passive" in the terminology of Leeper (1991), if the government shows strong scal discipline. If this is the case, we can design an optimal monetary policy rule without paying any attention to scal

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policy. However, if the economy is unstable in terms of the scal situation, it would be dangerous to choose a monetary policy rule independently of scal policy rules. For example, some researchers argue that the recent accumulation of public debt in Japan is evidence of a lack of scal discipline on the part of the Japanese government, and that it is possible that government bond market participants may begin to doubt the government's intention and ability to repay the public debt. If this is the case, we may need to take the future evolution of the scal regime into consideration when designing a monetary policy rule.

Against this background, the purpose of this paper is to estimate—scal policy feedback rules for Japan, the United States, and the United Kingdom for a period spanning more than a century, so as to gain a deeper understanding of the evolution of—scal policy regimes. One of the most important features of recent studies on—scal policy rules is the recognition that—scal policy regimes are not—xed over time, but evolve in a stochastic manner.¹ For example, Favero and Monacelli (2005) and Davig and Leeper (2007) estimate—scal policy rules for the United States during the postwar period under the assumption that there are two alternative—scal regimes, i.e., one with—scal discipline ("passive" regime) and the other one without—scal discipline ("active" regime), and that stochastic fluctuations between the two regimes may be characterized by a Markov process. They—nd that—scal regime switching occurred fairly frequently: Davig and Leeper (2007) report that there were twelve—scal regime changes during the period of 1948-2004, while Favero and Monacelli (2005) found that—scal policy was even more unstable than monetary policy.²

However, these pioneering works still have some shortcomings. First, they do not make an empirical distinction between *locally* and *globally* Ricardian policy rules. For example, Favero and Monacelli (2005) specify a locally Ricardian rule and ask whether the U.S. government has followed this rule or deviated from it. However, as pointed out by Bohn (1998) and Canzoneri et al. (2001), the transversality condition may be satisted even if the debt-GDP ratio does not follow a stationary process, or equivalently, even if a government deviates from a locally Ricardian policy rule. Second, the studies by Davig and Leeper (2007) and Favero and Monacelli (2005) do not pay much attention to governments' tax smoothing behavior. As pointed out by Barro (1986) and Bohn (1998), tax-smoothing

¹A comprehensive list of recent empirical studies on fiscal policy rules is provided by Afonso (2008).

²These studies are in sharp contrast with research on fiscal sustainability initiated by Hamilton and Flavin (1986) about two decades ago, which typically investigates whether fiscal variables such as the debt-GDP ratio are characterized by a stationary or a nonstationary process without any break (Trehan and Walsh (1988, 1991), Wilcox (1989), Ahmed and Rogers (1995)).

behavior may create a negative correlation between public debt and the primary surplus. Without properly controlling for such behavior when estimating a government's reaction function, researchers may easily obtain biased estimates of scal policy reactions to a change in public debt. Third, the empirical approach of these studies is based on maximum likelihood estimation and implicitly assumes that the debt-GDP ratio is stationary at least in the long run (i.e., that it is "Harris recurrent"). This condition is satis ed if, for example, the debt-GDP ratio switches between two AR (p) processes, one stationary and the other nonstationary, but the nonstationary regime is not visited too often or for too long (Francq and Zakoian (2001)). However, there is no a priori reason to believe that this condition is indeed satis ed for the debt-GDP ratio; it is possible that a non-Ricardian regime is visited frequently and/or for a long time, depending on the transition probabilities. If this is the case, maximum likelihood estimators will fail to follow a standard normal distribution even asymptotically (Douc et al. (2004)).³

We derive an estimating equation based on a model of optimal tax smoothing, paying particular attention to differences between locally and globally Ricardian rules, and then estimate the equation by the Bayesian method. The main ndings of the paper are as follows. First, the Japanese data set, covering the period 1885-2004, clearly rejects the view that the scal policy regime was xed throughout the sample period, i.e., that the Japanese government adopted only one policy stance -Ricardian or non-Ricardian - throughout the entire period. Rather, our empirical results suggest that the scal policy regime evolved over time in a stochastic manner, and that the debt-GDP ratio is well described by a Markov switching model with two or three states. Speci cally, Japanese scal policy is characterized by a locally Ricardian rule in 1885-1925 and 1950-1970. The former roughly corresponds to the period when Japan had adopted the gold standard, under which the government was forced to maintain a balanced budget. Japan left the gold standard in 1917. The latter period corresponds to the period of scal restructuring just after WWII, when the Japanese government, under the direction of the Supreme Commander for Allied Powers (SCAP) introduced a balanced budget system as part of the so-called "Dodge Line" in order to stop runaway inflation. On the other hand, Japanese scal policy is characterized by non-Ricardian rules in 1930-1950 and 1970-2004, suggesting that the Japanese government abandoned scal discipline not only during WWII, but also in the most recent

³Another important difference from the previous studies is that we use a unique dataset spanning more than a century. The use of this long horizon dataset makes us possible to detect slow mean reversion which is hard to find otherwise.

period starting in 1970. These empirical results are con rmed as being quite robust to changes in empirical speci cations.

Second, given that the Japanese debt-GDP ratio switches between stationary and nonstationary processes, one may wonder to what value the debt-GDP ratio goes to in the long run. To address this question, we conduct stochastic simulation exercises using the estimated transition probabilities, and nd that the debt-GDP ratio is quite likely to increase over the next 20 years, but will start declining after that and nally converge to zero. This implies that the debt-GDP process is "globally stationary" (i.e., stationary across regimes), although it may not necessarily be locally stationary (i.e., stationary within each regime). However, we also nd that this result is not very robust to changes in the speci cation of the estimating equation, such as the number of possible "states," and in some cases, we nd global nonstationarity.

Third, we apply our methodology to U.S. and U.K. data sets to nd that the scal behavior of the U.S. government throughout the entire sample period, 1840-2005, may be described as switching between locally Ricardian policy rules, while the behavior of the U.K. government during the entire sample period, 1830-2003, can be characterized as switching between globally Ricardian policy rules. Thus, the U.S. and U.K. results are in sharp contrast with the result for Japan. The U.S. result is consistent with Bohn (1998, 2008), but differs from Favero and Monacelli (2005) who report that U.S. government behavior deviated from Ricardian policy for most of their sample period, 1961-2002.

The remainder of this paper is organized as follows. Sections 2 and 3 explain our empirical approach, while Section 4 explains our data set. Section 5 presents the regression results. Section 6 concludes the paper.

2 Ricardian fiscal policy

2.1 The government's budget constraint

We start by looking at the government's budget constraint. Let us denote the nominal amount of public debt and base money at the end of period t by B_t and M_t . Also, we denote the one-period nominal interest rate starting in period t-1 by i_{t-1} , the nominal government expenditure (excluding interest payments) and the nominal tax revenue in period t by G_t and T_t . Then the consolidated flow

⁴The recent behavior of investors in the Japanese government bond market seems to be consistent with this as they show no hesitation to purchase government bonds even though the government is lacking fiscal discipline and rapidly accumulating public debt.

budget constraint of the government and the central bank takes the following form:

$$M_t + B_t = (1 + i_{t-1})B_{t-1} + M_{t-1} + (G_t - T_t).$$

Dividing both sides of this equation by nominal GDP, Y_t , we obtain:

$$m_t + b_t = \frac{1 + i_{t-1}}{1 + n_t} b_{t-1} + \frac{1}{1 + n_t} m_{t-1} - s_t,$$

where m_t , b_t , s_t , and n_t are defined by

$$m_t \equiv \frac{M_t}{Y_t}; \ b_t \equiv \frac{B_t}{Y_t}; \ s_t \equiv \frac{T_t - G_t}{Y_t}; \ n_t \equiv \frac{Y_t - Y_{t-1}}{Y_{t-1}}.$$

Denoting the total consolidated liabilities by $w_t (\equiv m_t + b_t)$, the transition equation for w_t can be expressed as:

$$w_t - w_{t-1} = \frac{i_{t-1}}{1 + n_t} w_{t-1} - \frac{n_t}{1 + n_t} w_{t-1} - \left[\frac{i_{t-1}}{1 + n_t} m_{t-1} + s_t \right]. \tag{1}$$

Note that $\frac{i_{t-1}}{1+n_t}m_{t-1}$ represents seignorage and that an increase in the primary surplus s_t or seignorage reduces total liabilities. Also note that an increase in the nominal growth rate n_t contributes to lowering total liabilities through the second term on the right-hand side, $-\frac{n_t}{1+n_t}w_{t-1}$, which is sometimes called the "growth dividend" (Bohn (2008)).

Equation (1) can be rewritten as

$$w_t = q_{t+1} \left[w_{t+1} + s_t \right] + \frac{i_t}{1 + i_t} m_t, \tag{2}$$

where q_t represents a discount factor that is de ned by

$$q_{t+1} \equiv \frac{1 + n_{t+1}}{1 + i_t}.$$

Iterating equation (2) forward from the current period and taking expectations conditional on information available in period t, we obtain a present-value expression of the budget constraint:

$$w_{t} = E_{t} \sum_{j=1}^{T} \left(\prod_{k=1}^{j} q_{t+k} \right) s_{t+j} + \frac{i_{t}}{1+i_{t}} m_{t} + E_{t} \sum_{j=1}^{T-1} \left(\prod_{k=1}^{j} q_{t+k} \right) \left(\frac{i_{t+j}}{1+i_{t+j}} \right) m_{t+j} + E_{t} \left(\prod_{k=1}^{T} q_{t+k} \right) w_{t+T}.$$

This implies that the transversality condition is given by

$$\lim_{T \to \infty} E_t \left(\prod_{k=1}^T q_{t+k} \right) w_{t+T} = 0. \tag{3}$$

2.2 Locally Ricardian policy rules

Woodford (1995) proposes that a scal policy commitment be called "Ricardian" if it implies that the transversality condition, equation (3), necessarily holds for all possible paths of endogenous variables (in particular, prices). More specifically, Woodford (1995, 1998) proposes two types of Ricardian scal policy rule.

The rst type, which is referred to as "locally Ricardian," can be expressed as

$$s_t + \frac{i_{t-1}}{1+n_t} m_{t-1} = \left[\lambda_t + \frac{i_{t-1}}{1+n_t} \right] w_{t-1} + \nu_t, \tag{4}$$

where λ_t is a time-varying parameter satisfying $0 < \lambda_t \le 1$, which represents the government's responsiveness to changes in total liabilities, and ν_t is an exogenous stationary variable. Note that the left-hand side of equation (4) represents the sum of the primary surplus and seignorage. Equation (4) requires the government to create a surplus in period t great enough to cover its interest payment in that period, $\frac{i_{t-1}}{1+n_t}w_{t-1}$.

By substituting (4) into (1), we can fully characterize the dynamics of w_t :

$$w_t = \left[1 - \lambda_t - \frac{n_t}{1 + n_t}\right] w_{t-1} - \nu_t.$$
 (5)

Under the assumption that n_t is an exogenous process (i.e., the government treats n_t as exogenously given when making a scal decision in period t),⁵ this equation implies that w_t would be a stationary process and thus satis es the transversality condition if the sum of λ_t and $\frac{n_t}{1+n_t}$ lies between zero and unity.⁶ Note that the assumption of a locally Ricardian policy requires that $1 - \lambda_t$ is smaller than unity, while stationarity of w requires that the coefficient on w_{t-1} in (5) is less than unity. These two conditions are closely related but not identical except for the case of $n_t = 0$.

An alternative speci cation to equation (4) would be:

$$s_t + \frac{i_{t-1}}{1+n_t} m_{t-1} + \frac{n_t}{1+n_t} w_{t-1} = \left[\hat{\lambda}_t + \frac{i_{t-1}}{1+n_t} \right] w_{t-1} + \nu_t.$$
 (6)

Note that $\hat{\lambda}_t \equiv \lambda_t + \frac{n_t}{1+n_t}$. Equations (4) and (6) are identical from a mathematical viewpoint, but they have different interpretations. Equation (6) implies that the government reduces the primary

⁵It is possible that n_t could be an endogenous variable in the sense that the government's fiscal behavior could have non-negligible consequences on the path of n_t . For example, as argued by Woodford (2001) among others, it might be possible that if the government does not react at all to changes in total liabilities (that is, $\lambda_t = 0$), then inflation endogenously emerges $(n_t > 0)$, and consequently the coefficient on w_{t-1} in equation (5) becomes less than unity.

⁶Note that, from an econometric point of view, w_t is a stationary process if the coefficient on w_{t-1} in equation (5) lies between -1 and 1 $(-1 < 1 - \lambda_t - \frac{n_t}{1+n_t} < 1)$. However, it seems safe to rule out the possibility that w converges over time to a constant value with oscillation, so that we can concentrate on the condition that the coefficient lies between 0 and 1 $(0 \le 1 - \lambda_t - \frac{n_t}{1+n_t} < 1)$.

surplus when the growth dividend is positive, for example, due to high inflation, and increases it when the growth dividend is negative; on the other hand, equation (4) requires the government to create a primary surplus independently of the level of the growth dividend. It can be easily seen that the transition equation corresponding to (5) is now given by

$$w_t = \left[1 - \hat{\lambda}_t\right] w_{t-1} - \nu_t,\tag{7}$$

and that w_t is a stationary process if $\hat{\lambda}_t$ satisfies the condition that $0 < \hat{\lambda}_t \le 1$.

Favero and Monacelli (2005) adopt a policy reaction function very close to equation (6). According to their denition, a government with scal discipline seeks to keep the primary decit lower than the "debt-stabilizing decit", which is given by

$$-\left[\frac{i_{t-1}}{1+n_t} - \frac{n_t}{1+n_t}\right] w_{t-1}.$$

Given this de nition, the debt-stabilizing de cit becomes positive if n_t takes a sufficiently large positive value, implying that the government can run a de cit.

2.3 Globally Ricardian policy rules

The idea that the government should maintain a surplus large enough to at least cover interest payments seems to be a useful one from a practical point of view,⁷ but the transversality condition does not necessarily require it. Speci cally, as shown by Bohn (1998) and Canzoneri et al. (2001), the transversality condition could be satisted even if the government reacts to an increase in total liabilities by less than the amount needed to cover its interest payments. This is the second type of Ricardian policy, which is referred to as "globally Ricardian."

Globally Ricardian policy can be expressed as

$$s_t + \frac{i_{t-1}}{1 + n_t} m_{t-1} = \gamma_t w_{t-1} + \nu_t, \tag{8}$$

where γ_t is a time-varying parameter satisfying $0 < \gamma_t \le 1$. Note that equations (4) and (6) require the government to generate a primary surplus that is sufficient to cover its interest payments in each period. Here, however, the government can now issue additional debt to pay interest on the existing

⁷If we rewrite equation (4) as $s_t - \frac{i_{t-1}}{1+n_t}b_{t-1} = \lambda_t w_{t-1} + \nu_t$, we see that the rule requires that not the primary surplus but the traditional fiscal surplus (i.e., primary surplus less interest payment) be adjusted in response to a change in total liabilities, which is the idea underlying the Maastricht Treaty and the Stability and Growth Pact. See Woodford (2001) for more on this issue.

debt at the beginning of that period. Under this policy rule, the dynamics of w_t are now given by

$$w_t = \left[1 - \gamma_t - \frac{n_t}{1 + n_t} + \frac{i_{t-1}}{1 + n_t}\right] w_{t-1} - \nu_t \tag{9}$$

or

$$w_t = \left[\frac{1}{q_{t-1}} - \gamma_t\right] w_{t-1} - \nu_t, \tag{10}$$

which implies that the transversality condition (equation (3)) is satis ed if $0 < \gamma_t \le \frac{1}{q_{t-1}}$. Note that this condition does not necessarily guarantee that w_t is a stationary process; in fact, it allows w_t to grow forever, but at a rate lower than the interest rate in each period. In that sense, a globally Ricardian rule imposes a weaker condition on government behavior than a locally Ricardian rule.

Bohn (1998, 2008) adopts a policy reaction function very close to equation (8) and looks at U.S. data to determine whether γ_t is positive. Equation (8) is an appropriate estimating equation when the government adopts a globally Ricardian policy or when it actually adopts a locally Ricardian policy but interest rates do not fluctuate much during the sample period. In the latter case, we would be able to empirically distinguish between a locally and a globally Ricardian policy just by looking at whether the estimated coefficient on w_{t-1} is greater than the sample average of the nominal interest rate. However, if the government adopts a locally Ricardian policy and fluctuations in interest rates are not small, then Bohn's specification may not be appropriate. For example, the estimated coefficient on w_{t-1} may become biased towards zero if fluctuations in interest rates are quite large during the sample period while those in public debt are negligibly small.

3 Estimation method

3.1 Estimating equations

Transition equations of government liabilities are given by (5) for the case of locally Ricardian, and by (9) for the case of globally Ricardian. We assume that the government stochastically switches between, say, locally Ricardian (i.e., λ in equation (5) is positive) and locally non-Ricardian (λ is zero or below zero). Similarly, the government switches between globally Ricardian (i.e., γ in equation (9) is positive) and globally non-Ricardian (γ is zero or below zero). These stochastic regime switches are

⁸Again, we rule out the possibility that the coefficient on w_{t-1} in (9) or (10) is below zero.

⁹However, Bohn (1998, 2008) does not consider the possibility that the fiscal regime evolves over time in a stochastic manner.

assumed to be described by a Markov switching model of the form

$$b_{t} = \begin{cases} \mu_{0} + (\alpha_{0} + \eta_{t})b_{t-1} + u_{0t} & \text{if} \quad S_{t} = 0\\ \mu_{1} + (\alpha_{1} + \eta_{t})b_{t-1} + u_{1t} & \text{if} \quad S_{t} = 1 \end{cases}$$

$$(11)$$

where $u_{it} = \varepsilon_{it} - \nu_t$ with $\varepsilon_{it} \sim i.i.d.$ $N(0, \sigma_i^2)^{.10}$ $\{S_t \in (0,1)\}$ is a two-state Markov chain with transition probabilities $p_{ij} = \Pr(S_t = j \mid S_{t-1} = i)$. For example, $S_t = 0$ and $S_t = 1$ correspond, respectively, to the regime with scal discipline and the regime without scal discipline. Note that public debt issued by the government b_t is used as the dependent variable rather than the total liabilities w_t in equations (5) and (9), following the previous studies on scal policy rules. This treatment is appropriate as a rst approximation if seignorage is small relative to primary surplus and government's scal behavior (i.e., government spending and taxation) is not affected much by it. However, it should be noted that ignoring seignorage may potentially create correlation between b_{t-1} and the error term, thereby yielding biased estimates.

We specify four different estimation equations based on different de nitions of η_t and ν_t .

Specification 1 $\eta_t = \nu_t = 0$: that is, equation (11) reduces to

$$b_t = \begin{cases} \mu_0 + \alpha_0 b_{t-1} + \varepsilon_{0t} & \text{if} \quad S_t = 0 \\ \mu_1 + \alpha_1 b_{t-1} + \varepsilon_{1t} & \text{if} \quad S_t = 1 \end{cases}$$

This is the benchmark case in which no exogenous variables are included. Hence, b_t follows a simple Markov-switching AR(1) process.

Specification 2 $\eta_t = 0$, and $\nu_t = -g_t^m$: that is, equation (11) becomes

$$b_t = \begin{cases} \mu_0 + \alpha_0 b_{t-1} + g_t^m + \varepsilon_{0t} & \text{if} \quad S_t = 0\\ \mu_1 + \alpha_1 b_{t-1} + g_t^m + \varepsilon_{1t} & \text{if} \quad S_t = 1 \end{cases}$$

This is a case in which government tax smoothing behavior is incorporated through g_t^m (military expenditures relative to GDP). As pointed out by Barro (1986) and Bohn (1998), the government's tax-smoothing behavior may create a negative correlation between public debt and the primary surplus.

 $^{^{10}}$ It is assumed that the error term, ε_{it} , is uncorrelated with b_{t-1} . A usual justification of this assumption is that b_{t-1} is predetermined. In this paper, we will employ this orthogonality assumption following the previous studies such as Bohn(1998). However, it should be noted that b_{t-1} may not necessarily be a predetermined variable but a forward-looking variable in some models. If this is the case, the coefficient on b_{t-1} is no longer consistently estimated because of the presence of endogeneity problem. See Li (2010) for more on this issue.

To illustrate this, consider a situation in which the government increases its expenditures, but only temporarily (such as in the case of a war). The government could increase taxes simultaneously by the same amount as the increase in expenditures, but it is costly to change marginal tax rates over time, since doing so increases the excess burden of taxation. Recognizing this, an optimizing government would seek to smooth marginal tax rates over time. This implies that a temporary increase in government expenditures would lead to a decrease in the primary surplus and an increase in public debt. Bohn (1998) argues that such a negative correlation between the primary surplus and public debt should be properly controlled for when estimating the government's reaction function; otherwise researchers may easily obtain imprecise estimates of scal policy reactions to an increase in public debt. Bohn (1998, 2008) shows that empirical results for the U.S. sharply differ depending on whether or not temporary government expenditures are included as an independent variable, while Iwamura et al. (2006) report a similar noting for Japan during the post-war period. Note that we impose the coefficient on g_t^m to be equal to unity in our speci cation, because tax smoothing argument implies that the size of a change in government expenditure and the size of a resulting change in primary surplus is almost identical.¹¹

Specification 3 $\eta_t = -\frac{n_t}{1+n_t}$, and $\nu_t = -g_t^m$: that is, equation (11) reduces to

$$b_{t} = \begin{cases} \mu_{0} + \left(\alpha_{0} - \frac{n_{t}}{1+n_{t}}\right) b_{t-1} + g_{t}^{m} + \varepsilon_{0t} & \text{if} \quad S_{t} = 0\\ \mu_{1} + \left(\alpha_{1} - \frac{n_{t}}{1+n_{t}}\right) b_{t-1} + g_{t}^{m} + \varepsilon_{1t} & \text{if} \quad S_{t} = 1 \end{cases}$$

This speci cation corresponds to equation (5) with $\alpha_i = 1 - \lambda_i$. Note that when n_t is very close to 0, speci cation 3 reduces to speci cation 2. This condition might hold in a very stable economy without any experience of high inflation, but unfortunately, this is not the case for Japan, which experienced three-digit inflation rates just after the end of WWII. Of course, Japan is not an exception, and one can easily not other examples in which the accumulation of public debt leads to uncontrollably high inflation. For such countries, speci cations 2 and 3 are not identical.

 $[\]overline{^{11}}$ As robustness check, we conducted the same estimation without imposing such a restriction on the coefficient of g_t^m . We confirm that the main results are not changed.

Specification 4 $\eta_t = -\frac{n_t}{1+n_t} + \frac{i_{t-1}}{1+n_t}$, and $\nu_t = -g_t^m$: that is, equation (11) reduces to

$$b_{t} = \begin{cases} \mu_{0} + \left(\alpha_{0} - \frac{n_{t}}{1+n_{t}} + \frac{i_{t-1}}{1+n_{t}}\right) b_{t-1} + g_{t}^{m} + \varepsilon_{0t} & \text{if} & S_{t} = 0 \\ \mu_{1} + \left(\alpha_{1} - \frac{n_{t}}{1+n_{t}} + \frac{i_{t-1}}{1+n_{t}}\right) b_{t-1} + g_{t}^{m} + \varepsilon_{1t} & \text{if} & S_{t} = 1 \end{cases}$$

This corresponds to equation (9) with $\alpha_i = 1 - \gamma_i$. This speci cation differs from speci cation 3 in that interest payments, $\frac{i_{t-1}}{1+n_t}$, are included in η_t , reflecting the fact that the government is not required to create surplus to cover its interest payments. Note that a globally Ricardian policy requires α_i to be less than unity, implying that, when n_t is always equal to zero, b_t could continue to grow forever, but at a rate lower than the borrowing cost in each period.

Later in Section 5, we will estimate each of the four equations shown above; we will pay a particular attention to the speci cations 3 and 4, each of which describes the scal behavior of a government with scal discipline (i.e. locally or globally Ricardian) and tax smoothing motivation.

3.2 Estimation

We estimate equation (11) by employing a Bayesian approach via the Gibbs sampler instead of a classical approach based on maximum likelihood estimation. The Bayesian approach has the following advantages. First, the maximum likelihood estimator (MLE) has the potential disadvantage that inference on S_t is conditional on the estimates of the unknown parameters. We estimate the parameters of the model and then make inferences on S_t conditional on the estimates of the parameters as if we knew for certain the true values of the parameters. In contrast, the Bayesian approach allows both the unknown parameters and S_t to be random variables. Therefore, inference on S_t is based on the joint distribution of the parameters and S_t (see Kim and Nelson (1999)).

Second, for the Markov switching models, the likelihood is often not uni-modal but multi-modal. Therefore, numerical algorithms such as Expectation Maximization (EM) and Newton-Rapson algorithms sometimes converge to a local maximum on the likelihood surface. This is a typical problem encountered with data in practice, regardless of which optimization algorithms are used. Maddala and Kim (1998) argue that the maximum likelihood estimation method is fragile as multiple local maxima are often found.

Third, MLE follows a non-standard limiting distribution when the process is nonstationary in the long run (or globally nonstationary). To our knowledge, such limiting distributions have not been

derived for Markov-switching models. On the other hand, the Bayesian method can approximate the joint and marginal distributions of the parameters and S_t via a Markov chain Monte Carlo (MCMC) simulation method such as the Gibbs sampler. The method is valid even when the observed process exhibits non-stationarity (or explosive) behavior in the long run (see Sims (1988)). To illustrate this point, let us suppose there are two scal policy regimes: one is a stable regime in which the debt-GDP ratio is characterized by a stationary process, and the other one is an unstable regime in which the debt-GDP ratio is characterized by a nonstationary process. Note that the mere existence of an unstable regime does not necessarily imply global instability: The system could still be globally stable if the unstable regime is not visited too often or for too long. In this sense, the transition probabilities of the Markov chain are important determinants of global stability or instability. On the other hand, as shown by Francq and Zakoian (2001), it is possible that the system is globally unstable even when both of the two regimes are stable. An important point to be emphasized here is that it would not be appropriate to employ MLE if it is uncertain whether the system is globally stable.¹²

3.3 MCMC simulation

The rst time the Gibb sampler was used in a Bayesian analysis of Markov switching models was in the study by Albert and Chib (1993). The Gibbs sampler is used to approximate the joint and marginal distributions of the parameters of interest from the conditional distributions of the subsets of parameters given the other parameters (see Kim and Nelson (1999) for an introduction to Gibbs sampling). It is useful in this case because the joint distributions are difficult to obtain.

We follow Kim and Nelson (1999) to estimate a model of the form:

$$b_t^* = \begin{cases} \mu_0 + \alpha_0 b_{t-1} + \varepsilon_{0t}, & \text{if} & S_t = 0\\ \mu_1 + \alpha_1 b_{t-1} + \varepsilon_{1t}, & \text{if} & S_t = 1 \end{cases}$$

where $b_t^* = b_t - \eta_t b_{t-1} + \nu_t$ and $\varepsilon_{it} \sim i.i.d.N(0, \sigma_i^2)$ for i = 0, 1 with $\sigma_{S_t}^2 = \sigma_0^2(1 + h_1 S_t)$ and $h_1 > 0$. $\{S_t \in (0, 1)\}$ is a two-state Markov chain with transition probabilities $p_{ij} = \Pr(S_t = j \mid S_{t-1} = i)$. Note that the two states are assumed to be identified not by α_{S_t} but by $\sigma_{S_t}^2$, simply because we want to know if there is any difference between the two states in terms of α_{S_t} .

 $^{^{12}}$ An alternative empirical framework to study fiscal regime shifts would be to use the methodology proposed by Bai and Perron (1998), in which a multiple linear regression model with l breaks (or l+1 regimes) is examined within the classical framework. However, this approach requires the process to be weakly stationary in each regime. Therefore, their method cannot be applied in our context.

3.3.1 Prior distributions

Next we describe the choice of priors for the unknown parameters. Let $\tilde{h}_1 = 1 + h_1$ with $h_1 > 0$. Then the priors are the following:

$$\mu_i \sim N(\psi, \omega^{-1}), \quad \alpha_i \sim N(\phi, c^{-1}),$$

$$\sigma_0^2 \sim IG(\frac{v}{2}, \frac{\delta}{2}), \quad \widetilde{h}_1 \sim IG(\frac{v}{2}, \frac{\delta}{2})_{1(\widetilde{h}_1 > 1)},$$

$$p_{11} \sim beta(u_{11}, u_{10}), \quad p_{00} \sim beta(u_{00}, u_{01})$$

The parameters used are $\psi = 0$, $\omega = 25$, $\phi = 0$, c = 1, $(v, \delta) = (0, 0)$, $u_{00} = u_{11} = 8$, and $u_{10} = u_{01} = 2$. Hence the prior of σ_i^2 is non-informative. The other parameters are chosen so that the priors are informative but relatively diffused.¹³ The means and standard deviations of the prior distributions are presented in the following table.

Priors for the parameters

	Distribution	Mean	Std. Dev.
μ_i	Normal	0.00	0.20
α_i	Normal	0.00	1.00
p_{ii}	Beta	0.80	0.12
$rac{\sigma_0^2}{\widetilde{h}_1}$	Inverted Gamma		_
\widetilde{h}_1	Inverted Gamma	_	_

3.3.2 Computational algorithm

The needed posterior conditional distributions for implementing Gibbs sampling are easily obtained from the priors and the assumptions of the data generating process. The following steps 1 through 5 are iterated to obtain the joint and marginal distributions of the parameters of interest.

Step 1: Generate p_{11} and p_{00} conditional on $\widetilde{S}_T = (S_1, ..., S_T)$. Let n_{ij} refer to the total number of transitions from state i to j, which can be counted from \widetilde{S}_T . Then

$$p_{11} \mid \widetilde{S}_T \sim beta(u_{11} + n_{11}, u_{10} + n_{10})$$

 $p_{00} \mid \widetilde{S}_T \sim beta(u_{00} + n_{00}, u_{01} + n_{01})$

¹³We tried alternative prior specifications as a robustness check, and confirmed that the basic results of the paper are not sensitive to prior specifications.

Step 2: Generate μ_i conditional on \widetilde{S}_T , σ_i^2 , and α_i . We have the regression $y_t = \mu_i + \varepsilon_{it}$ where $y_t = b_t^* - \alpha_i b_{t-1}$ for $t \in \{t : S_t = i\}$. Hence, the posterior distribution is $\mu_i \sim N(\psi_*, \omega_*^{-1})$ where

$$\omega_* = \sum_{t \in \{t: S_t = i\}} 1/\sigma_i^2 + \omega, \ \psi_* = \omega_*^{-1} \left[\sum_{t \in \{t: S_t = i\}} y_t/\sigma_i^2 + \omega \psi \right]$$

Step 3: Generate α_i conditional on \widetilde{S}_T , σ_i^2 , and μ_i . Let $d_t^* = b_t^* - \mu_i$, then we have the regression $d_t^* = \alpha_i b_{t-1} + \varepsilon_{it}$ for $t \in \{t : S_t = i\}$. Hence, the posterior distribution is $\alpha_i \sim N(\phi_{i*}, c_{i*}^{-1})$ where

$$c_{i*} = \sum_{t \in \{t: S_t = i\}} b_{t-1}^2 / \sigma_i^2 + c, \ \phi_{i*} = c_{i*}^{-1} \left[\sum_{t \in \{t: S_t = i\}} b_{t-1} d_t^* / \sigma_i^2 + c\phi \right]$$

Step 4: Generate σ_0^2 and σ_1^2 conditional on \widetilde{S}_T , μ_i , and α_i . We rst generate σ_0^2 conditional on h_1 and then generate $\widetilde{h}_1 = 1 + h_1$ to indirectly generate σ_1^2 . Conditional on h_1 , the posterior distribution of σ_0^2 is as follows:

$$\sigma_0^2 \sim IG\left(\frac{v_{0*}}{2}, \frac{\delta_{0*}}{2}\right)$$

where

$$v_{0*} = v + T$$

$$\delta_{0*} = \delta + RSS_0 + RSS_1/(1 + h_1)$$

with $RSS_i = \sum_{t \in \{t: S_t = i\}} (b_t^* - \mu_i - \alpha_i b_{t-1})^2$. Conditional on σ_0^2 , the posterior distribution of $h_1 = 1 + h_1$ is as follows:

$$\widetilde{h}_1 \sim IG\left(\frac{v_{1*}}{2}, \frac{\delta_{1*}}{2}\right)_{1(\widetilde{h}_1 > 1)}$$

where

$$v_{1*} = v + T_1$$

$$\delta_{1*} = \delta + RSS_1/\sigma_0^2$$

with $T_1 = \sum_{t=1}^{T} S_t$. Once \tilde{h}_1 is obtained, we can calculate σ_1^2 .

Step 5: Generate $\widetilde{S}_T = (S_1, ..., S_T)$ conditional on the other parameters. This is conducted using multi-move Gibbs sampling, which was rst introduced by Carter and Kohn (1994) in the context of a state-space model. Here the procedure for generating \widetilde{S}_T using the multi-move Gibbs-sampling is the same as that in Kim and Nelson (1999).

We iterate steps 1 through 5 M+N times and discard the realizations of the rst M iterations but keep the last N iterations to form a random sample of size N on which statistical inference can be made. M must be sufficiently large so that the Gibbs sampler converges. Also, N must be large enough to obtain the precise empirical distributions. Taking these aspects into consideration, we set M=5000 and N=10000.

4 Data

We construct a data set covering the period 1885-2004 for Japan, 1840-2005 for the United States, and 1830-2003 for the United Kingdom. Data frequency is annual.¹⁴

4.1 Japan

Public debt Public debt is de ned as the amount of gross debt issued by the central and local governments at the end of each scal year.¹⁵ To convert the gures reported in various budget documents into a format consistent with the SNA, we make adjustments by excluding the amount of debt issued under the Colonial Special Accounts and the Public Enterprise Special Accounts, both of which are outside the general government according to the SNA de nition.¹⁶

Nominal GDP A single data set covering the entire sample period is not available, so that we collect data from various sources and link them in a consistent way. For the period after FY1936, we use a data set produced by the Japanese government (various versions of the SNA), while for the period before FY1935, we basically use Ohkawa et al. (1974). However, since data are completely missing for the nal stage of WWII (FY1944 and 1945), we estimate the real GDP in these two years by using the index of industrial production and the index of agriculture, forestry and shery

 $^{^{14}\}mathrm{See}$ the appendix of Ito et al. (2011) for details. All data we use are available upon request.

¹⁵The data for the debt issued by the central government are taken from various documents published by the Ministry of Finance, including "Japanese Government Bonds Statistics," "The Financial History of the Meiji and Taisho Period in Japan," the "Annual Report on Japanese Government Bonds Statistics," and "Budget Statistics," while the data for the debt issued by local governments is taken from documents issued by the Ministry of Finance and the Ministry of Home Affairs (Ministry of Internal Affairs and Communications), including "The Financial History of the Meiji and Taisho Period in Japan," "Local Government Bonds Statistics," the "Annual Publication on Local Public Finance," and the "Annual Report on Local Public Finance Statistics."

¹⁶We use various definitions of the general government: For 1885-1954, we use the definition by the Economic Counsel Board, for 1995-1969, the OLD SNA, for 1970-1979, the 68SNA, and for 1980-2004, the 93SNA. Note that these definitions slightly differ from each other, because special accounts held by the central government and business accounts held by local governments are sometimes classified as part of the general government and sometimes not.

production,¹⁷ and the GDP deflator by using the agricultural price index, the production goods price index, and the consumer price index.

Government interest payments The data for government interest payments for FY1885 to 1929 are taken from Emi and Shionoya (1966) for FY1885 to 1929, while those for FY1952 to 2004 are from various documents published by the government, including the "White Paper on National Income," the "Annual Report on National Income Statistics," and the "Annual Report on National Accounts." As for the period between FY 1930 and FY1951, we estimate interest payments closely following the methodology adopted by Emi and Shionoya (1966).

Military expenditure For the years after FY1947, we use the gures referred to as "National Defense and Related Affairs" in various issues of the "Settlement of General Account Revenues and Expenditures" published by the Ministry of Finance. The data for FY1946 are taken from Economic Counsel Board (1954), while for the years before FY1946, we use the data from Emi and Shionoya (1966).

As for military spending during wartime, that is, FY1937 to FY1945, we dene this as expenditures spent only by the forces at home, and do *not* include expenditures spent by the forces overseas. This is consistent with our denition of public debt in which those debts issued under the ve Colonial Special Accounts (namely, the Chosen Government, Taiwan Government, Kwantung Office, Karafuto Office, and Nanyo Office) are *not* included.¹⁸

4.2 The U.S. and the U.K.

For the United States, the data are taken from the "Historical Statistics of the United States" (Carter et al. (2006)) and the "Historical Tables, Budget of the United States Government" published by the Office of Management and Budget. For the United Kingdom, the data sources are the "British"

¹⁷This methodology closely follows the one used by the Japanese central bank in its various publications on financial and economic activities around the end of WWII (see, for example, Bank of Japan (1950)).

¹⁸However, as one might imagine, a non-negligible portion of expenditures spent by the forces *overseas* was financed by the central government through the issue of public debt, especially at the final stage of WWII. Ideally, this portion should be included in our definition of military expenditure, but we do not do so because reliable figures for that portion are not available. However, to see how sensitive our empirical results are to this treatment of military expenditures, we created an alternative series of military expenditures using a tentative estimate by Emi and Shionoya (1966) for military spending by the forces overseas that were financed by the central government through the Colonial Special Accounts, and repeated the same empirical exercise as in Section 5. We were able to confirm that the basic empirical findings are not sensitive to the definition of military spending.

Historical Statistics" (Mitchell (1988)), the "Annual Abstract of Statistics" published by the Office for National Statistics, and the Public Sector Finances Databank by HM Treasury.

5 Empirical results

5.1 Preliminary analysis

The trend in the debt-GDP ratio for Japan, the U.S., and the U.K. is shown in Figure 1. We see that there are three major periods of debt accumulation in Japan. The rst period, 1904 to 1905, is the period of the Russo-Japanese War (1904-1905). Reflecting a substantial increase in military expenditure, the debt-GDP ratio increased to over 50 percent at the end of 1905; however, it started to decrease again right after the end of the war and the decline continued until, in 1918, the debt-GDP ratio had returned to the pre-war level. Given that there was no remarkable growth dividend during this period (the nominal growth rate in 1906-1915 was 5.4 percent per year on average), one can see that this downward trend mainly came from scal reconstruction, including substantial spending reductions. As pointed out by many researchers, the government during this period had a strong political will to restore budget balance so as to avoid the risk of a massive outflow of gold under the gold standard system.

The second phase of debt accumulation was 1920 to 1944, i.e., the period that includes WWII. The increase in the debt-GDP ratio accelerated following the outburst of war with China in 1937, and the ratio eventually reached 1.8 when the war ended in 1945. However, as can be seen in Figure 1, the debt-GDP ratio dropped precipitously right after the end of the war, all the way to a level very close to zero. This is an episode of inflationary erosion of the debt, or "partial default," due to hyper-inflation during this period.²⁰

Finally, the most recent phase of debt accumulation started in the early 1970s and continues until today. A series of reforms in the social security system, including the introduction of indexation in the public pension system, have been implemented since the Tanaka administration declared a changeover to the welfare state in 1973. This accumulation of debt continued until the government – nally started scal reconstruction in the latter half of the 1980s, including a substantial cut in spending and the introduction of a consumption tax in 1989. However, the debt-GDP ratio started to increase again in

¹⁹Although Japan won the war, it received no war reparations from Russia.

²⁰The rate of inflation in terms of the GDP deflator was 273 percent in 1945, 175 percent in 1946, and 154 percent in 1947.

the 1990s, at least partially due to the collapse of the asset price bubble in the early 1990s.

In Table 1, we decompose changes in the debt-GDP ratio into four components: the contribution of primary de cit; the contribution of interest charge; the contribution of real GDP growth; and the contribution of inflation. Focusing on the three phases in which the debt-GDP ratio declined, we see the following. The rst phase, 1906 to 1916, is the period immediately after the end of the Russo-Japanese war. The debt-GDP ratio declined by 4.3 percent per year. Importantly, it came mostly from a reduction of primary de cit, implying that the scal reconstruction during this period was a successful one. On the other hand, the decline of the debt-GDP ratio in 1945 to 1948 was much larger than that in the preceding phase, but this came not from a reduction of primary de cit but from inflation. Finally, the debt-GDP ratio declined in 1987 to 1990 by 2 percent per year. The contribution of primary de cit was -2.2 percent, suggesting that scal reconstruction was going on during this period. However, public debt had already reached at a very high level at this time, thus the contribution of interest charge was high. As a result, the contribution of de cit with interest, which is de ned as the sum of the contribution of primary de cit and the contribution of interest charge, was positive, contributing to an increase (rather than a decrease) in the debt-GDP ratio. This is sharply contrasted with what happened during the scal reconstruction in 1906-1916. The debt-GDP ratio did decline in 1987-1990, but it mainly came from high economic growth.

Turning to the U.S. and the U.K., we see that the main cause of debt accumulation was increases in military expenditures during wartime. Speci-cally, the U.S. debt-GDP showed a rapid and substantial increase in 1861-66, 1916-19, and 1941-46, respectively corresponding to the Civil War, WWI, and WWII periods. The debt-GDP ratio for the U.K. is also characterized by three spikes, created by the Napoleonic War, WWI, and WWII. A notable difference with the Japanese data is that in both of these countries there was no major inflation comparable to Japan's hyper-inflation in 1945-47. It should also be noted that the U.S. and the U.K. have never experienced an uncontrollable accumulation of public debt during peacetime, which again is in sharp contrast with the Japanese experience since the early 1970s.

5.2 Empirical results for Japan

Table 2 presents the regression results for Japan obtained from a two-state model. Panel A of the table shows a benchmark regression in which no exogenous variables are included (namely, specication 1).

The estimate of α in regime 0 is 0.517, indicating that the debt-GDP ratio is characterized by a stationary process that converges to its mean quite quickly. On the other hand, the estimate of α in regime 1 is 1.116. Since its lower bound (1.067) exceeds unity, we cannot reject the null that the debt-GDP ratio follows an explosive process.²¹ Figure 2 presents the estimated probability of regime 1 in each year of the sample period, as well as the estimated coefficient on b_{t-1} , which is calculated as a weighted average of the coefficients in regimes 0 and 1, with the estimated probabilities of each regime being used as a weight. The shaded area represents the 95 percent con dence interval. Figure 2 shows that the years except 1945-1970 fall under regime 1 and that the coefficient on b_{t-1} exceeds unity except during the period 1945-1970.

Panel B of Table 2 shows the results of a similar regression, but this time we added military expenditures as an exogenous variable (speci cation 2). Again, the debt-GDP ratio is characterized by a stationary process for regime 0 and an explosive process for regime 1. The estimated coefficient on b_{t-1} , shown in Figure 2, looks quite similar to the previous case, except that the coefficient is now lower than unity in 1890-1905 (the period of the Sino-Japanese and the Russo-Japanese Wars) and 1915-1920 (the period of WWI).

Panel C of Table 2 reports the regression result for the case in which military expenditure and the growth dividend, $-\frac{n_t}{1+n_t}b_{t-1}$, are included as exogenous variables (speci cation 3). Again, we see that regime 0 is characterized by a stationary process and regime 1 by an explosive process. But a notable difference from the previous two speci cations is that the estimate of α in regime 0 is now much closer to unity, indicating that convergence to its mean is much slower. Speci cally, the estimate of α in speci cation 1 (0.5177) implies that the debt-GDP ratio declines to half of its initial value after about 1.05 years, while the one in speci cation 3 (0.9178) implies that the half-life is 8.08 years. The surprisingly quick decline in the debt-GDP ratio found in speci cations 1 and 2 mainly reflects the fact that the debt-GDP ratio fell very quickly during the hyper-inflation period in 1945-47. This problem is now xed by properly controlling for the growth dividend. Figure 2 now shows that the probability of regime 1 is close to unity in 1930-1950 and 1970-2004, while the probability of regime 0 is high in 1885-1925 and 1950-1970. These results suggest that the former periods are characterized by a locally Ricardian rule.

²¹Note that the estimate of the constant terms μ is below zero, implying that b explodes to negative infinity if b starts at an extremely low level. However, this is unlikely to occur, given that the estimate of μ is very close to zero, and not significantly different from zero.

Finally, Panel D of Table 2 reports the results for the case in which military expenditure and $\left(\frac{i_{t-1}}{1+n_t} - \frac{n_t}{1+n_t}\right)b_{t-1}$ are included as exogenous variables (speci cation 4). The results are basically the same as those for speci cation 3, except that the estimates of α in regimes 0 and 1 are both lower, con rming that the assumption of a globally Ricardian policy is weaker than that of a locally Ricardian policy.

In sum, we nd that the Japanese government made several large changes with respect to its scal behavior over the past 120 years. Speci cally, Japanese scal policy is characterized by a locally Ricardian rule in 1885-1925 and 1950-1970. The former largely corresponds to the period in which Japan had adopted the gold standard under which the government was forced to maintain a balanced budget until Japan left the gold standard in 1917, following the same move by the core countries of the system.²² The second period follows the scal restructuring ushered in December 1948, when SCAP instructed the Japanese government to implement a balanced budget in order to stop runaway inflation.²³ On the other hand, Japanese scal policy is characterized by a non-Ricardian rule in 1930-1950 and 1970-2004, suggesting that the Japanese government abandoned scal discipline not only during WWII, but also in the most recent period starting in 1970.²⁴

5.3 Sensitivity analysis

AR (2) model The baseline regressions reported in Table 2 assume that the government adjusts the primary surplus in period t in response to a change in public debt at the beginning of period t. Given that we use annual data, this seems to be a good approximation to actual policy making. However, as often pointed by researchers and practitioners, it usually takes more than one year before scal decisions are nally made. If this is the case, our baseline speci cation may not be appropriate. To address this potential problem, we extend our baseline AR(1) model (equation (11)) to an AR(K)

 $^{^{22}}$ See Shizume (2001) for more on the Japanese government's fiscal behavior during the gold standard period.

²³For details on the "Dodge Line," see, for example, Cohen (1950) and Yamamura (1967).

²⁴Markov switching models, including our model given by equation (11), are based on the assumption of recurring states. This may not be an appropriate way to describe the evolution of fiscal policy rules. For example, the Ricardian rule in 1885-1925 may not necessarily be identical to the one in 1950-70. It is beyond the scope of this paper to fully address this issue, but we estimated a random coefficient model, in which the estimating equation is given $b_t = \mu + (\alpha_t - \frac{n_t}{1+n_t} + \frac{i_{t-1}}{1+n_t})b_{t-1} + g_t^m + \epsilon_t$, where α_t follows a random walk process ($\alpha_t = \alpha_{t-1}$ + disturbance). The regression result shows that α exceeds unity (i.e. non-Ricardian rule) in 1945, 1965-1985, and 1995-2004, and stays below unity for the other years. This is basically the same as our baseline result.

model of the form

$$b_{t} = \begin{cases} \mu_{0} + (\alpha_{0} + \eta_{t})b_{t-1} + \sum_{k=1}^{K-1} \theta_{0k} \triangle b_{t-k} + u_{0t} & \text{if} & S_{t} = 0\\ \mu_{1} + (\alpha_{1} + \eta_{t})b_{t-1} + \sum_{k=1}^{K-1} \theta_{1k} \triangle b_{t-k} + u_{1t} & \text{if} & S_{t} = 1 \end{cases}$$

Note that this speci-cation differs from a partial adjustment model, such as the one adopted by Favero and Monacelli (2005), in that the coefficient on lagged values of b depends only on the current regime (and not on past regimes). We conducted a lag search to end up with K = 2. The results of the regressions using this equation are reported in Table 3 and Figure 3 and are basically the same as before. In addition, the coefficient on $\triangle b_{t-1}$, denoted by θ in Table 3, is very close to zero in each regime, indicating that the AR (1) speci-cation is not a binding constraint.

Net public debt The baseline regressions use gross public debt issued by the central and local governments rather than net debt. This is based on the assumption that governments own only a small amount of nancial assets and that fluctuations in the amount of nancial assets over time are insubstantial. However, as pointed out by Broda and Weinstein (2005), Japan's public sector, through its social security funds, holds non-negligible amounts of nancial assets. According to their estimate, net debt held by the Japanese public sector at the end of FY2002 was equivalent to 64 percent of GDP, while the corresponding gross—gure was 161 percent. Obviously, the difference is not trivial.

To evaluate how sensitive the baseline results are, we re-estimate our equations replacing gross debt with net debt. The net debt data we use here are the data published by the Economic and Social Research Institute (ESRI), Cabinet Office, which cover the general government, including the central and local governments and the social security funds. Unfortunately, however, the ESRI data cover only the postwar period starting in 1955, so that the estimation is conducted only for this shorter sample period.

Figure 4 compares Japanese general government gross and net debt. Although the difference between the two in terms of the vertical distance is indeed substantial, we still see a common long-term trend: Namely, both start to increase around 1970 and basically continue to rise over the next 35 years. Comparing the estimation result reported in Table 4 with the baseline result (Table 2), we see no change in that the debt-GDP ratio is characterized by a stationary process in regime 0 and a nonstationary process in regime 1. We may therefore safely conclude that our baseline results are not

particularly sensitive to the de nition of public debt.

Somewhat interestingly, however, if one looks closely at Figure 5, one can see a substantial decline in the probability of regime 1 during the latter half of the 1980s. Correspondingly, the coefficient on b_{t-1} fell below unity during this period in speci-cation 3 and more clearly in speci-cation 4.25 The latter half of the 1980s famously is a period of scal reconstruction during which the Japanese government intensively cut expenditure to achieve the target of "no net issuance of government bonds." One may interpret the decline in the coefficient on b_{t-1} during this period as reflecting the restoration of scal discipline. However, the coefficient on b_{t-1} started to increase again in the early 1990s and has remained very close to unity since.

Automatic stabilizers Recent empirical studies on scal policy rules emphasize the importance of automatic stabilizers in explaining fluctuations in the scal surplus/de cit (see Taylor (2000), Auerbach (2003), and Bohn (1998)). For example, Taylor (2000), using U.S. data for 1960-1999, nds that the cyclical surplus was highly correlated with fluctuations in the output gap but this was not necessarily the case for the structural surplus. To control for this effect in our regression exercise, we add the output gap to the estimating equations. Speci cally, we closely follow Barro (1986) and Bohn (1998) by introducing a new variable, $YVAR_t$, which is de ned as $YVAR_t \equiv (1 - Y_t/Y_t^*)(G_t^*/Y_t)$, where Y_t is the real GDP, Y_t^* is its trend component estimated by HP lter, and G_t^* is the trend component of real government spending. The regression results presented in Table 5 show that the coefficient on YVAR is around 0.7 and signi-cantly different from zero in both speci-cations, indicating that automatic stabilizers did play an important role even in the Japanese case. However, the coefficient of main interest to us, α , is almost the same as before, suggesting that the baseline result is not sensitive to whether we control for the output gap or not.

²⁵These results are quite different from the ones reported in Section 5.2, which is based on the gross debt data. One may regard this difference coming from the difference in the definition of debts, i.e., gross versus net debts. To see this, we run the same set of gross-debts regressions as in Section 5.2, but we now use a shorter sample period starting in 1955, which is the same starting period for the net-debts regressions in Table 4 and Figure 5. The results (not reported here) indicate that the probability of regime 1 fell substantially during the latter half of the 1980s, which is identical to the finding from Figure 5. This implies that the difference for the latter half of the 1980s comes not from the difference in the definition of debts, but from the difference in the sample period.

 $^{^{26}\}mathrm{See},$ for example, Ihori et al. (2001) for more on fiscal reform efforts during this period.

 $^{^{27}}$ Figure 5 shows that the coefficient on b_{t-1} during the latter half of the 1980s is slightly below unity but not statistically different from unity in specification 3, while it is significantly smaller than unity in specification 4. This implies that the fiscal regime during this period is characterized not by a locally Ricardian but a globally Ricardian rule. This result is perfectly consistent with the fact that the government indeed aimed at "no net issuance of government bonds" but had little intention of going further than that, i.e., it had no intention to reduce the debt-GDP ratio to a lower level or even zero.

No restriction on the coefficient on interest payments As we can see from equations (4) and (8), the sole difference between locally and globally Ricardian rules is what kind of restriction we impose on the coefficient on interest payments $\frac{i_{t-1}}{1+n_t}w_{t-1}$. Locally Ricardian rules impose the restriction that the coefficient should be equal to unity, while globally Ricardian rules impose the restriction that it should be zero. The former corresponds to speci cation 3, while the latter corresponds to speci cation 4. An important implication of these restrictions, whether the coefficient should be zero or unity, is that these speci cations allow a switching only between locally Ricardian rules and other rules (i.e., rules that do not belong to locally Ricardian rules) in the case of speci cation 3, and a switching only between globally Ricardian rules and the other rules in the case of speci cation 4. These speci cations would be inappropriate if, for example, policy switching occurs between locally and globally Ricardian rules.

To deal with this potential problem, we conduct a similar regression as before but now do not impose an a priori restriction on the coefficient on interest payments. Speci cally, we add a new independent variable $\frac{i_{t-1}}{1+n_t}b_{t-1}$ to equation (11) with

$$\eta_t = -\frac{n_t}{1 + n_t}; \ \nu_t = -g_t^m.$$

The coefficient on the new independent variable should be close to zero if the true rule is well approximated by a locally Ricardian rule, and it should be unity in the case of a globally Ricardian rule. The results are shown in Table 6 and indicate that the estimated coefficient is 0.628 in regime 0 (the stationary regime) and 0.506 in regime 1 (the nonstationary regime). More importantly, the lower bound in regime 0 is 0.235, rejecting the null of zero, while the upper bound in regime 0 is slightly lower than unity (0.990), again rejecting the null of unity. This means that the true rule is not well approximated by the two extremes (i.e., locally and globally Ricardian rules) but is located between them. The same results can be seen for regime 1.²⁸ However, the estimated values of α in Table 6 tend to fall between those obtained in speci cations 3 and 4 of Table 2, con rming that the main results regarding—scal policy behavior in Table 2 hold without any substantial modi cations.

Three-state model The robustness of the ndings in Table 2 are examined in Table 7 by extending the analysis to a three state model. Panel A, which reports the regression results for speci cation 3,

 $^{^{28}}$ These results suggest that neither empirical studies focusing only on locally Ricardian rules nor those focusing only on globally Ricardian rules employ an appropriate estimating equation.

shows that regime 0 is characterized by a stationary process ($\alpha = 0.914$), regime 1 by an explosive process ($\alpha = 1.084$), and regime 2 by another highly explosive process ($\alpha = 1.301$). Figure 8 shows that the periods falling under regime 1 in Figure 2 are again classi ed as regime 1,²⁹ suggesting that the number of regimes allowed in Table 2 (namely, two regimes) is not an inappropriate description of the true model. These results, together with the results for speci cation 4, more or less con rm the earlier ndings: (1) the periods 1885-1920 and 1950-1970 fall under regime 0 (a regime with scal discipline); (2) the period 1920-1950 falls under regime 1 (a regime without scal discipline).

5.4 Are debt ratios globally stationary or nonstationary?

The regression analysis in this section seeks to determine whether the debt-GDP ratio follows a stationary process within a regime. However, as we discussed earlier, even if the ratio is stationary within a regime, this does not necessarily imply that it is stationary in the long run. This is simply because regime changes occur stochastically in accordance with transition probabilities. Thus, what we need to know is where the debt-GDP ratio is headed in the long run given the estimated transition probabilities, or, put differently, we need to know whether its distribution converges over time to a certain distribution. A process is said to be globally stationary if the distribution converges to a certain distribution over time, while stationarity within a regime is called local stationarity. Global stationarity implies that the effect of policy shocks on the debt-GDP ratio becomes smaller and smaller over time and nally disappears in the long run. Investors in government bonds markets are interested in whether this global stationarity is satis ed or not, and policymakers, especially central banks, are interested in this property when designing monetary policy rules.

Francq and Zakoian (2001) obtain a result regarding the relationship between local and global stationarity that is of some interest in the present context, namely that local stationarity is neither a necessary nor a sufficient condition for global stationarity. For example, suppose there are two regimes and one satis es local stationary while the other does not. Even in this combination, the process could be globally stationary. On the other hand, even if each of the two regimes satis es local stationarity, this does not necessarily imply global stationarity.³⁰

As we saw in Table 2, the regression results using a two-state model show that one regime satis es

 $^{^{29}}$ The exceptions are 1944 and 1970-1980, years in which the debt-GDP ratio recorded an extremely high growth rate, so that they are classified as regime 2.

³⁰Gali (2007) provides a clear and interesting discussion of the implications of Francq and Zakoian's (2001) result on the determinacy of an equilibrium in a monetary economy.

(local) stationarity while the other one does not. Also, as we saw in Table 7, the regression results using a three-state model indicate that one regime satis es (local) stationarity, but the other two do not. Given these results, one may wonder if they imply global stationarity or nonstationarity. To address this issue, we conduct the following simulation exercise. We generate a time series of b_t using

$$b_{t} = \begin{cases} \hat{\mu}_{0} + \left(\hat{\alpha}_{0} - \frac{n_{t}}{1+n_{t}}\right) b_{t-1} + u_{0t}, & \text{if} \quad S_{t} = 0\\ \hat{\mu}_{1} + \left(\hat{\alpha}_{1} - \frac{n_{t}}{1+n_{t}}\right) b_{t-1} + u_{1t}, & \text{if} \quad S_{t} = 1 \end{cases}$$

for a two-state model and the corresponding equation for a three-state model. Here, each parameter with a hat represents the posterior mean of the estimates in the earlier regressions. More specifically, we randomly draw policy shocks and policy regimes using the parameters and transition probabilities obtained from the regression of specification 3 and generate a replication for the time series of the debt-GDP ratio over 1000 years for various paths of the nominal growth rate (n_t) that are exogenously determined. We repeat this process 5000 times to obtain a distribution of the debt-GDP ratio in every year of the 1000 years. We can say that the debt-GDP process is globally stationary if this distribution is stable over time; otherwise it is globally nonstationary.

Table 8 reports the rst, second, and third quartiles of the simulated distribution with T = 500 (500 years later) and T = 1000 for the two-state and three-state models. In Panel A it is assumed that the initial regime is a stationary one (i.e., $S_0 = 0$), and that the debt-GDP ratio in period 0 is zero. On the other hand, in Panel B, it is assumed that the initial regime is a nonstationary one $(S_0 = 1)$ and that the initial debt-GDP ratio is unity (100 percent). The simulation results from the two-state model show that the distribution is stable over time, irrespective of the initial conditions and the assumed values of nominal growth rates (n), clearly indicating that the debt-GDP ratio satis es global stationarity. On the other hand, the results from the three-state model show that the distributions with T = 500 and T = 1000 differ significantly for the case of n = 0.00, 0.03, and 0.06, implying that the process is globally nonstationary.³¹

Figure 9 presents a similar simulation conducted to forecast the future path of the debt-GDP ratio over the next 100 years. To make the initial condition as close to the current situation in Japan as possible, we assume that the initial regime is $S_0 = 1$ and that the debt-GDP ratio in period 0 is 1.7, which is the actual—gure at the end of 2004. According to the result from the two-state model with

 $^{^{31}}$ However, when n goes up to 0.10, the distributions with T=500 and T=1000 become identical, suggesting that sufficiently high nominal growth could make the debt-GDP ratio globally stationary. The threshold for nominal growth rates is about 8 percent, which is lower than the sample average (13.7 percent).

3 percent nominal growth, the "third quartile" line goes up until it reaches 3 with T=20, indicating that a further increase in the debt-GDP ratio is quite likely to occur over the next 20 years. After that, however, the debt-GPD ratio enters a declining trend as a result of the switch to a stationary regime and then converges to a quite narrow (and probably tolerable) band within 100 years. On the other hand, the result from the three-state model with 3 percent nominal growth shows that the median of the distribution increases quite quickly to reach an unrealistic and intolerable level within 50 years, and that its variance increases over time, clearly indicating global nonstationarity.

5.5 Empirical results for the U.S.

Table 9 presents the regression results for the United States using a two state model. Results for speci cation 3, presented in Panel A, indicate that each of the regimes, 0 and 1, is characterized by a stationary process. This implies that the U.S. government's scal behavior during the sample period can be described as a switching between locally Ricardian policy rules. If we turn to the results for speci cation 4, presented in Panel B, they again indicate that each regime, 0 and 1, satis es stationarity, implying that U.S. scal policy is characterized by a switching between globally Ricardian rules.

These results suggest that the U.S. government's scal behavior consistently has been very close to locally Ricardian policy throughout the entire sample period. In fact, the estimated coefficient on b_{t-1} , presented in Figure 10, consistently and statistically significantly remains below unity. If we compare these results with those reported in previous studies on U.S. scal policy, we and some similarities. Bohn (2008), for example, regressed the U.S. primary surplus on public debt for a sample period from 1793 to 2003 and reports that the OLS estimate of the coefficient on public debt is positive and significantly different from zero when tax smoothing effects are properly controlled for. Bohn interprets this result as providing evidence for a globally Ricardian rule; but since the estimated coefficient is typically greater than the average interest rate level, this could be interpreted as suggesting a rule that is even locally Ricardian. Bohn (1998) conducts a similar exercise using data for 1916-1995 and nds that the coefficient on public debt is significantly positive not only for the entire sample period, but also for ve sub-sample periods, including the postwar period. These results reported by Bohn (1998, 2008) are consistent with ours.

Favero and Monacelli (2005) estimate an equation that is very close to our speci cation 1 (equation

(6)) using the maximum likelihood method and report that U.S. government behavior has been deviating from Ricardian policy for most of the entire sample period (1961-2002), except that it was close to a locally Ricardian rule during the period of 1995-2001. Although their results cannot be directly compared to ours because the empirical methodologies differ in several respects, we still attempt to do so by adjusting our sample period to theirs. Panels C and D of Table 9 show the results of a regression that is similar to that underlying Panels A and B, but that now uses data for the postwar period. The regression results indicate that the estimate of α in regime 0 is less than unity, suggesting that it is a stationary regime as before, but that the upper bound of α in regime 1 slightly exceeds unity, so that we fail to reject the null of a unit root. Fluctuations in the estimated coefficient on b_{t-1} , presented in Figure 10, show that it has been slightly higher than unity since 1975, implying the possibility that the U.S. government started to deviate from Ricardian policy around 1975. However, the gure clearly shows that the estimated coefficient on b_{t-1} is consistently less than unity during the period before 1975 and that there is no evidence for the return to Ricardian policy around 1995 that Favero and Monacelli (2005) detected. Thus, there are certain inconsistencies between their results and ours. 32

Given that U.S. scal policy is characterized by switching between stationary regimes, we may apply a model with multiple breaks, as proposed by Bai and Perron (1998), to the U.S. data. This model does not require researchers to assume that policy regime switching is a recurrent phenomenon, and that it has a Markov property. This is an important advantage, but on the other hand it requires the debt process to be weakly stationary in each regime, so that we cannot apply it to the Japanese data. The regression results reported in Table 10 show that regime changes occur four times (i.e., there are ve different regimes) with both speci cations 3 and 4. According to the result for speci cation 4, the estimate of α is slightly higher than unity during the wartime period (regime 3, 1917-1943) but is signi cantly smaller than unity in the other four regimes. These results may be interpreted as con rming our earlier results obtained from the Markov switching regression.³³

 $^{^{32}}$ We also estimated specification 1, which is very close to the estimating equation employed by Favero and Monacelli (2005), for the entire sample period as well as for the postwar period, but found that both regimes are stationary ones. 33 However, the results for specification 3 are not very informative since α exceeds unity in three out of the five regimes. This result may be interpreted as evidence against applying the Bai-Perron method even to the U.S. data.

5.6 Empirical results for the U.K.

Table 11 presents the regression results for the United Kingdom using a two-state model. Results for speci cation 3 indicate that regime 0 is characterized by a stationary process, while regime 1 is characterized by a unit root process (the upper bound of α slightly exceeds unity). On the other hand, results for speci cation 4 indicate that both regime 0 and regime 1 are characterized by a stationary process, implying that the U.K. government's scal behavior is characterized by switching between globally Ricardian rules.

6 Conclusion

This paper estimated scal policy feedback rules in Japan, the United States, and the United Kingdom for more than a century and allowing for stochastic regime changes. By estimating a Markov switching model by the Bayesian method, we arrived at the following ndings. First, the Japanese data clearly reject the view that the scal policy regime has been xed, i.e., that the Japanese government has adopted a regime that is either Ricardian or non-Ricardian throughout the entire period. Rather, our results indicate a stochastic switch of the debt-GDP ratio between stationary and nonstationary processes and thus a stochastic switch between Ricardian and non-Ricardian regimes. Speci cally, Japanese scal policy was characterized by a locally Ricardian rule in 1885-1925 and 1950-1970 but by a non-Ricardian rule in 1930-1950 and 1970-2004. Second, through simulation exercises using the estimated parameters and transition probabilities, we showed that the debt-GDP ratio may be nonstationary even in the long run (i.e., globally nonstationary). Third, the Japanese result stands in sharp contrast with the results for the U.S. and the U.K., which indicate that in these countries, government scal behavior has been consistently characterized by Ricardian policy.

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Table 1: Decomposition of Changes in Japan's Debt-GDP Ratio

	Change in Debt-GDP Ratio	Contribution of Primary Deficit	Contribution of Interest Charge	Contribution of Real Growth	Contribution of Inflation
1886-2004	0.3	2.4	1.7	-0.7	-3.1
1886-1905	1.4	1.8	1.1	-0.7	-0.8
1906-1916	-4.3	-3.7	2.4	-1.3	-1.7
1917-1944	4.3	6.3	2.1	-0.9	-3.2
1945-1948	-46.2	3.2	0.8	6.3	-56.6
1949-1986	1.0	1.4	1.1	-0.8	-0.7
1987-1990	-2.0	-2.2	3.2	-2.3	-0.7
1991-2004	6.3	3.9	2.7	-0.9	0.6

Table 2: Two-State Model for Japan

Panel A: Speci cation 1

	Regime 0			Regime 1		
	LB	Mean	UB	LB	Mean	UB
$\overline{\mu}$	0.0355	0.0512	0.0669	-0.0549	-0.0267	0.0023
α	0.4783	0.5177	0.5529	1.0674	1.1168	1.1649
σ^2	0.0006	0.0010	0.0018	0.0037	0.0050	0.0068
p_{11}	0.9193	0.9658	0.9941			
p_{00}	0.7804	0.9078	0.9811			

Panel B: Speci cation 2

	Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB	
μ	0.0380	0.0535	0.0688	-0.0863	-0.0591	-0.0321	
α	0.3785	0.4134	0.4476	1.0424	1.0821	1.1233	
σ^2	0.0005	0.0009	0.0015	0.0024	0.0033	0.0044	
p_{11}	0.8978	0.9564	0.9900				
p_{00}	0.7706	0.8984	0.9792				

Panel C: Speci cation 3

	Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0133	0.0036	0.0164	-0.0300	0.0073	0.0476	
α	0.8681	0.9178	0.9762	1.0167	1.0641	1.1110	
σ^2	0.0003	0.0005	0.0007	0.0022	0.0033	0.0049	
p_{11}	0.8552	0.9378	0.9867				
p_{00}	0.8778	0.9448	0.9864				

Panel D: Speci cation 4

	Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0067	0.0056	0.0169	-0.0524	-0.0150	0.0193	
α	0.8126	0.8550	0.8998	1.0103	1.0536	1.1003	
σ^2	0.0003	0.0004	0.0006	0.0022	0.0033	0.0050	
p_{11}	0.8631	0.9440	0.9876				
p_{00}	0.8921	0.9469	0.9831				

Note: The transition probability, p_{ij} , represents $\Pr(S_t = j \mid S_{t-1} = i)$. The columns labeled "LB" and "UB" refer to the lower and upper bound of the 95% confidence interval and the columns labeled "Mean" refer to the mean of the marginal distribution of the parameter.

Table 3: AR(2) Model

Panel A: Speci cation 3

		Regime 0		Regime 1			
	LB	Mean	UB	LB	Mean	UB	
μ	-0.0088	0.0069	0.0185	-0.0298	0.0075	0.0383	
α	0.8572	0.9004	0.9578	1.0151	1.0558	1.1028	
θ	0.0218	0.1227	0.3150	-0.0099	0.1009	0.1999	
σ^2	0.0003	0.0004	0.0006	0.0020	0.0030	0.0045	
p_{11}	0.8782	0.9454	0.9883				
p_{00}	0.8752	0.9412	0.9827				

Panel B: Speci cation 4

		Regime 0		Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0058	0.0079	0.0189	-0.0489	-0.0125	0.0248	
α	0.8007	0.8429	0.8933	0.9979	1.0449	1.0871	
θ	0.0317	0.1213	0.2190	-0.0024	0.0854	0.1745	
σ^2	0.0002	0.0004	0.0005	0.0019	0.0030	0.0045	
p_{11}	0.8689	0.9467	0.9855				
p_{00}	0.8868	0.9439	0.9876				

Table 4: Net Public Debt

Panel A: Speci cation 3

		Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB		
μ	-0.0333	-0.0213	-0.0144	0.0075	0.0276	0.0415		
α	0.7131	0.9227	0.9916	0.9916	1.0311	1.0737		
σ^2	0.0001	0.0002	0.0003	0.0002	0.0005	0.0010		
p_{11}	0.7812	0.9040	0.9783					
p_{00}	0.7321	0.8799	0.9674					

Panel B: Speci cation 4

		Regime 0		Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0276	-0.0211	-0.0140	-0.0009	0.0202	0.0356	
α	0.7961	0.8822	0.9412	0.9770	1.0185	1.0572	
σ^2	0.0001	0.0002	0.0003	0.0003	0.0005	0.0009	
p_{11}	0.7855	0.9052	0.9788				
p_{00}	0.7159	0.8701	0.9583				

Table 5: Automatic Stabilizers

Panel A: Speci cation 3

		Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB		
The coefficient	0.4700	0.7765	1.1077	0.3547	0.7559	1.1602		
on $YVAR$								
μ	-0.0103	0.0031	0.0163	-0.0263	0.0152	0.0564		
α	0.8696	0.9192	0.9631	1.0117	1.0598	1.1073		
σ^2	0.0003	0.0005	0.0007	0.0024	0.0039	0.0061		
p_{11}	0.8603	0.9397	0.9879					
p_{00}	0.8903	0.9482	0.9851					

Panel B: Speci cation 4

		Regime 0		Regime 1			
	LB	Mean	UB	LB	Mean	UB	
The coefficient	0.4811	0.8034	1.1901	0.3282	0.7032	1.1213	
on $YVAR$							
μ	-0.0073	0.0067	0.0188	-0.0514	-0.0099	0.0323	
α	0.8054	0.8505	0.9008	0.9992	1.0483	1.0948	
σ^2	0.0003	0.0004	0.0006	0.0025	0.0040	0.0062	
p_{11}	0.8626	0.9423	0.9880				
p_{00}	0.8796	0.9459	0.9875				

Table 6: No Restriction on the Coefficient on Interest Payments

		Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB		
The coefficient on interest payments	0.2351	0.6283	0.9907	0.1046	0.5064	0.8778		
μ	-0.0088	0.0052	0.0174	-0.0431	-0.0062	0.0336		
α	0.8228	0.8772	0.9367	1.0155	1.0617	1.1075		
σ^2	0.0003	0.0004	0.0006	0.0022	0.0033	0.0048		
p_{11}	0.8668	0.9420	0.9884					
p_{00}	0.8826	0.9454	0.9850					

Table 7: Three-State Model

Panel A: Speci cation 3

		Regime 0			Regime 1			Regime 2	
	LB	Mean	UB	LB	Mean	UB	LB	Mean	UB
$\overline{\mu}$	-0.0423	0.0018	0.0220	-0.0552	-0.0277	0.0205	-0.3044	-0.0300	0.0394
α	0.8520	0.9140	1.0612	1.0434	1.0844	1.1171	1.0959	1.3019	1.4832
σ^2	0.0001	0.0003	0.0006	0.0005	0.0007	0.0011	0.0006	0.0083	0.0121
p_{00}	0.7802	0.9072	0.9777						
p_{01}	0.0077	0.0571	0.1645						
p_{02}	0.0015	0.0357	0.1146						
p_{10}	0.0023	0.0407	0.1138						
p_{11}	0.8346	0.9237	0.9766						
p_{12}	0.0048	0.0357	0.0973						
p_{20}	0.0016	0.0637	0.2323						
p_{21}	0.0183	0.1344	0.3110						
p_{22}	0.5847	0.8019	0.9426						

Panel B: Speci cation 4

		Regime 0			Regime 1			Regime 2	
	LB	Mean	UB	LB	Mean	UB	LB	Mean	UB
μ	-0.0271	0.0125	0.0261	-0.0731	-0.0560	-0.0040	-0.0642	-0.0242	0.0170
α	0.7960	0.8364	0.9461	1.0327	1.0799	1.0996	1.1787	1.2730	1.3424
σ^2	0.0001	0.0003	0.0005	0.0004	0.0006	0.0009	0.0005	0.0030	0.0063
p_{00}	0.8001	0.9016	0.9761						
p_{01}	0.0078	0.0576	0.1435						
p_{02}	0.0034	0.0408	0.1085						
p_{10}	0.0037	0.0433	0.1117						
p_{11}	0.8413	0.9256	0.9768						
p_{12}	0.0041	0.0311	0.0879						
p_{20}	0.0015	0.0543	0.1974						
p_{21}	0.0342	0.1430	0.3168						
p_{22}	0.5978	0.8027	0.9418						

Table 8: Globally Stationary or Nonstationary?

Panel A: $S_0 = 0$ and $b_0 = 0$

	Two	o-State Mo	del	Thr	ee-State Mo	del				
Quartile	First	Median	Third	First	Median	Third				
0% Grow	th									
T = 500	-0.1471	0.0006	0.1525	-1.1E+10	-3.1117	1.4E + 10				
T=1000	-0.1593	-0.0007	0.1497	-2.5E+21	-2.7E+07	2.6E + 21				
3% Grow	3% Growth									
T=500	-0.0751	0.0005	0.0772	-3.6E + 04	0.0414	4.9E + 04				
T=1000	-0.0790	-0.0011	0.0786	-5.9E+09	0.6536	1.1E + 10				
6% Grow	h									
T=500	-0.0569	0.0003	0.0574	-4.2741	-0.0016	4.4939				
T=1000	-0.0591	-0.0012	0.0584	-16.665	0.0085	20.506				
10% Grov	wth									
T=500	-0.0476	0.0001	0.0463	-0.1160	0.0008	0.1205				
T=1000	-0.0478	-0.0006	0.0466	-0.1175	0.0010	0.1192				
10.707 C	.1									
13.7% Gr										
T=500	-0.0423	-0.0003	0.0413	-0.0579	0.0013	0.0615				
T=1000	-0.0428	-0.0004	0.0403	-0.0598	-0.0001	0.0592				

Panel B: $S_0 = 1$ and $b_0 = 1$

			0			
	Twc	State Mo	del	Thr	ee State M	odel
Quartile	First	Median	Third	First	Median	Third
0% Grow	th					
T = 500	-0.1476	0.0017	0.1623	6.1E + 08	2.9E + 11	8.9E + 13
T=1000	-0.1524	-0.0028	0.1515	$1.0E{+}19$	5.2E+22	1.8E + 26
3% Grow	h					
T=500	-0.0800	-0.0007	0.0780	131.32	1.7E + 05	7.2E + 07
T=1000	-0.0780	-0.0007	0.0751	4.2E + 05	1.3E+10	9.2E + 13
6% Grow	th.					
T=500	-0.0573	-0.0003	0.0582	-0.2212	0.4199	121.10
T=1000	-0.0575	0.0006	0.0582 0.0585	-0.2212	0.4199 0.2312	359.11
1-1000	-0.0010	0.0000	0.0505	-1.0212	0.2312	555.11
10% Grov	vth					
T = 500	-0.0481	-0.0007	0.0467	-0.1082	0.0011	0.1195
T=1000	-0.0458	0.0007	0.0467	-0.1131	0.0006	0.1172
13.7% Gr	owth					
		0.0000	0.0416	0.0602	0.0000	0.0574
T=500	-0.0427	-0.0009	0.0416	-0.0603	-0.0009	0.0574
T=1000	-0.0400	0.0008	0.0413	-0.0573	0.0013	0.0600

Note: We randomly draw policy shocks and policy regimes using the parameters obtained from regressions of specification 3 and generate 5000 replications for the time series of the debt-GDP ratio (1000 years) for various paths of the nominal growth rate (n_t) , which are exogenously determined. The figures in the table represent the first, second, and third quartiles of the simulated distribution with T=500 (i.e., 500 years later) and T=1000. The average growth rate over the entire sample was 13.7 percent.

Table 9: Two-State Model for the U.S.

Panel A: Speci cation $3,\,1840\text{-}2005$

		Regime 0		Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0039	-0.0013	0.0014	0.0055	0.0242	0.0458	
α	0.8734	0.8805	0.8885	0.9025	0.9393	0.9760	
σ^2	0.00003	0.00007	0.0001	0.0004	0.0007	0.0010	
p_{11}	0.8448	0.9161	0.9702				
p_{00}	0.8635	0.9287	0.9704				

Panel B: Speci cation 4, 1840-2005

	Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0031	-0.0012	0.0008	0.0062	0.0277	0.0518	
α	0.8448	0.8526	0.8594	0.8432	0.8811	0.9165	
σ^2	0.00003	0.00005	0.00007	0.0007	0.0010	0.0014	
p_{11}	0.8101	0.8922	0.9530				
p_{00}	0.8637	0.9243	0.9644				

Panel C: Speci cation 3, 1948-2004

	Regime 0			Regime 1			
	LB	Mean	UB	LB	Mean	UB	
$\overline{\mu}$	-0.0426	-0.0111	0.0114	-0.0182	0.0085	0.0332	
α	0.8478	0.8887	0.9441	0.9261	0.9699	1.0189	
σ^2	0.00005	0.0001	0.0002	0.0002	0.0004	0.0006	
p_{11}	0.8250	0.9273	0.9849				
p_{00}	0.7771	0.9068	0.9777				

Panel D: Speci cation 4, 1948-2004

	Regime 0				Regime 1			
	LB	Mean	UB	LB	Mean	UB		
$\overline{\mu}$	-0.0522	-0.0300	-0.0073	-0.0443	-0.0245	-0.0057		
α	0.8492	0.8907	0.9285	0.9330	0.9653	1.0004		
σ^2	0.00005	0.0001	0.0002	0.0001	0.0002	0.0004		
p_{11}	0.8379	0.9292	0.9833					
p_{00}	0.7636	0.9024	0.9794					

Table 10: Multiple Break Tests for the U.S.

Panel A: Speci cation 3

Panel B: Speci cation 4

	-			-	
	μ	α		μ	α
Regime 1	-0.0093	0.9555	Regime 1	-0.0120	0.9167
1840 - 1872	(0.0026)	(0.0240)	1840 - 1872	(0.0028)	(0.0256)
Regime 2		1.0009	Regime 2		0.9781
1873-1916		(0.0265)	1873-1916		(0.0283)
Regime 3		1.0469	Regime 3		1.0264
1917-1943		(0.0125)	1917-1943		(0.0133)
Regime 4		0.9071	Regime 4		0.8868
1944 - 1972		(0.0057)	1944 - 1972		(0.0061)
Regime 5		1.0135	Regime 5		0.9450
1973 - 2004		(0.0079)	1973-2004		(0.0084)

Note: The constant term is imposed to be identical across regimes. The maximum number of breaks is 5 with ϵ =0.15. Figures in parentheses denote standard errors.

Table 11: Two-State Model for the U.K.

Panel A: Speci cation 3

	Regime 0			Regime 1			
•	LB	Mean	UB	LB	Mean	UB	
μ	0.0837	0.1026	0.1220	-0.0341	-0.0264	-0.0180	
α	0.8043	0.8213	0.8369	0.9884	0.9955	1.0019	
σ^2	0.0003	0.0004	0.0005	0.0004	0.0005	0.0006	
p_{11}	0.9128	0.9544	0.9817				
p_{00}	0.6603	0.8175	0.9248				

Panel B: Speci cation 4

	Regime 0				Regime 1			
	LB	Mean	UB	LB	Mean	UB		
$\overline{\mu}$	-0.0033	0.0692	0.0952	-0.0411	-0.0336	-0.0239		
α	0.7986	0.8202	0.8686	0.9640	0.9709	0.9773		
σ^2	0.0003	0.0004	0.0005	0.0003	0.0004	0.0006		
p_{11}	0.9027	0.9474	0.9816					
p_{00}	0.6323	0.7900	0.9199					

Figure 1: Public Debt (Relative to Nominal GDP)

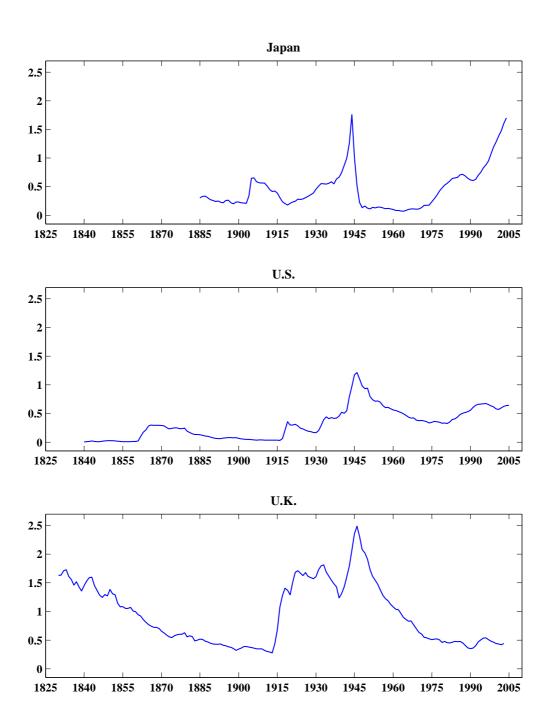
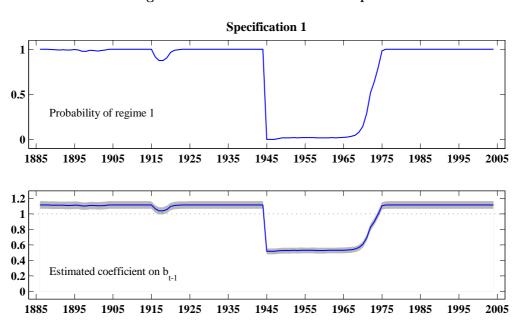


Figure 2: Two-State Model for Japan



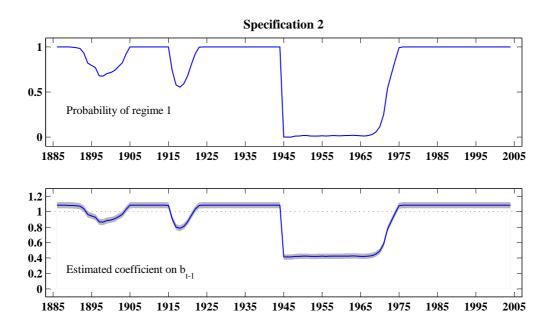
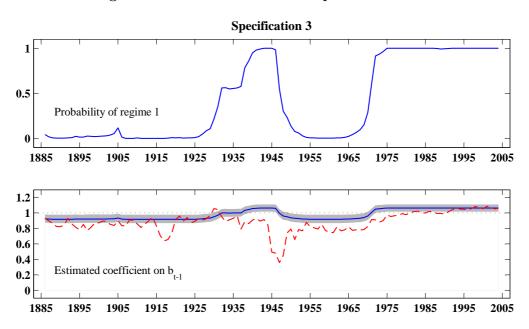


Figure 2: Two-State Model for Japan—Continued



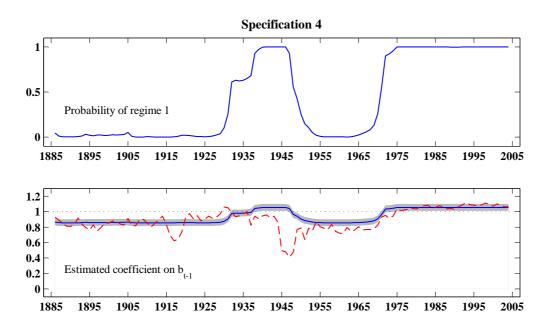
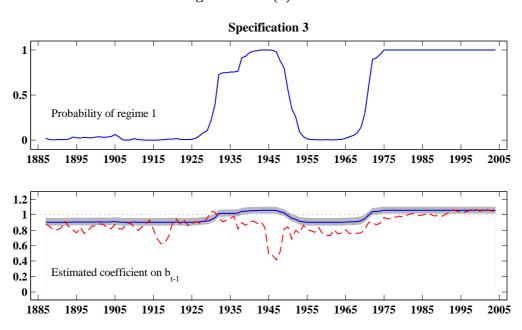


Figure 3: AR(2) Model



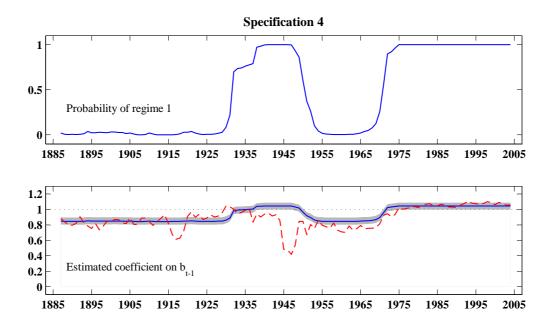
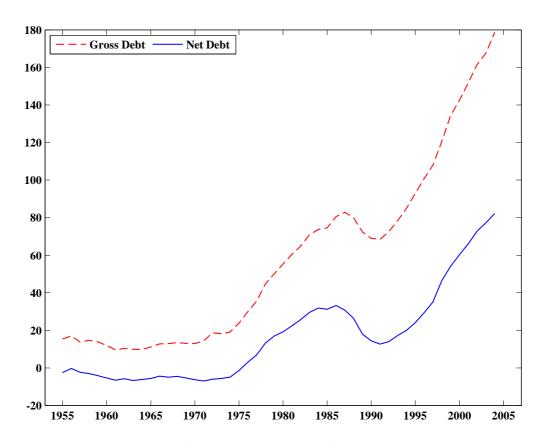
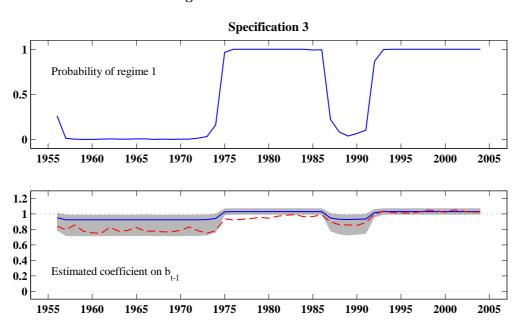


Figure 4: Net Public Debt in Japan (Relative to Nominal GDP)



Sources: Economic Planning Agency, $Report\ on\ National\ Accounts,\ 1955$ to 1969, and Cabinet Office, $Annual\ Report\ on\ National\ Accounts.$

Figure 5: Net Public Debt



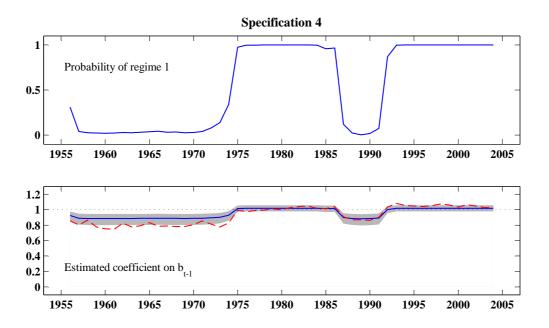
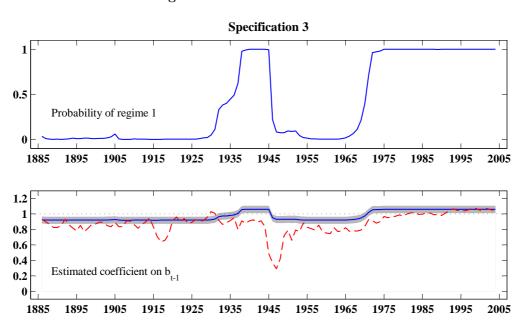


Figure 6: Automatic Stabilizers



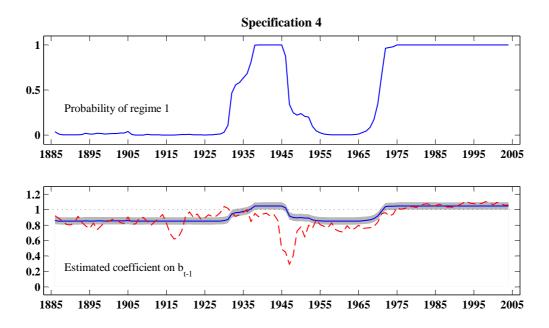


Figure 7: No Restriction on the Coefficient on Interest Payments

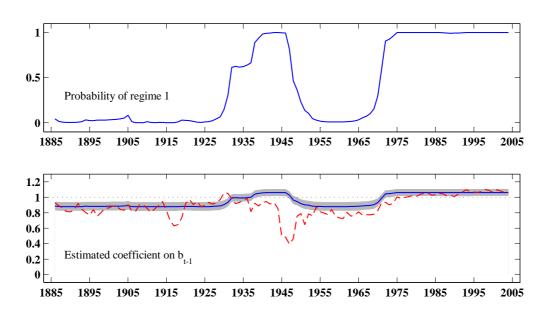


Figure 8: Three-State Model for Japan

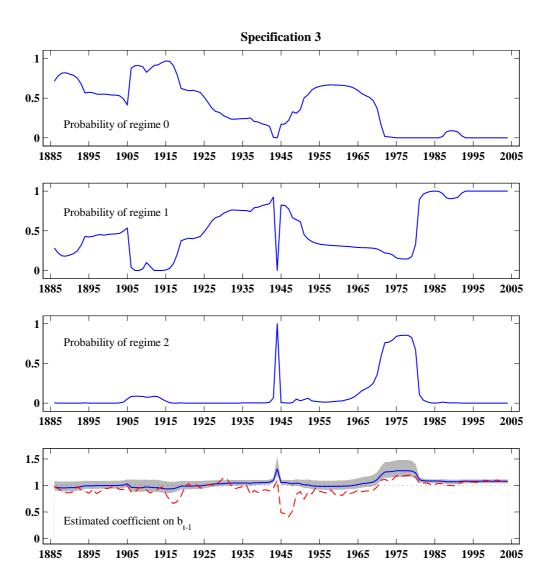


Figure 8: Three-State Model for Japan—Continued

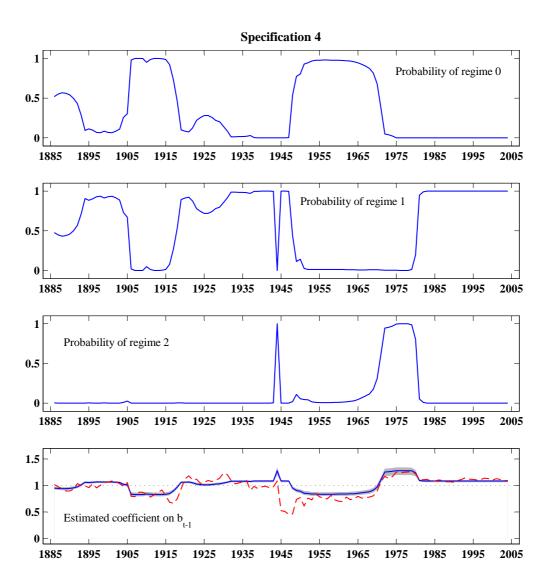
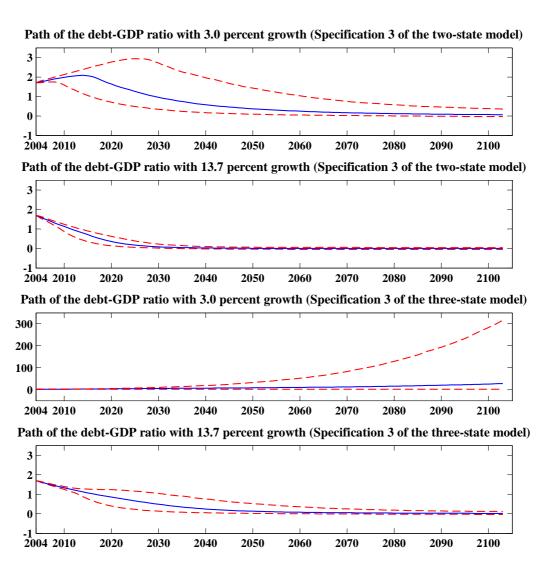
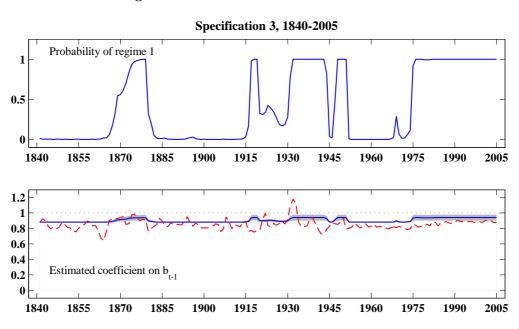


Figure 9: Globally Stationary or Nonstationary?



Note: The data of size 120 are generated from Specification 3 using estimated values with $b_0 = 1.7$ and $S_0 = 1$. In all cases, we replicate this procedure 5000 times to compute the first, second, and third quartiles.

Figure 10: Two-State Model for the U.S.



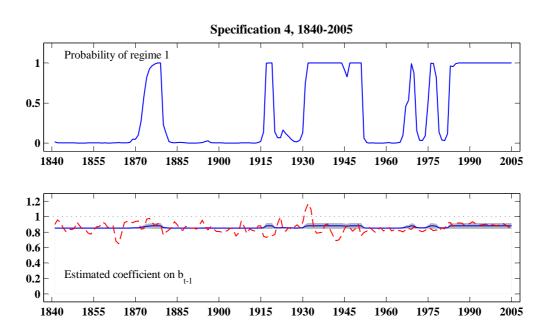
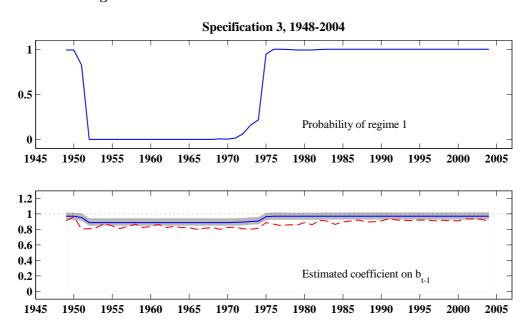


Figure 10: Two-State Model for the U.S.—Continued



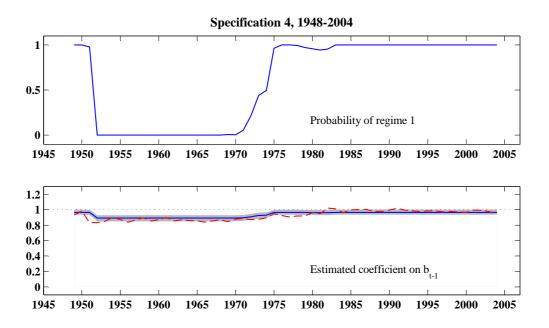


Figure 11: Two-State Model for the U.K.

